

## HW #11c

### Math 182, Spring 2009

Due Friday, May 1, 2009, by 11:00 a.m.

1. Check the validity of the maximum principle for the harmonic function

$$u(x, y) = \frac{4 - x^2 - y^2}{4 - 4x + x^2 + y^2}$$

in the domain  $D = \{x^2 + y^2 \leq 1\}$ .

2. A function  $u(x, y)$  is subharmonic in a domain  $D$  if  $\Delta u \geq 0$  in  $D$ . Let  $D$  be a bounded domain. Show that the maximum of a subharmonic function  $u$  in  $\overline{D}$  occurs on the boundary of  $D$ ,  $\partial D$ .