## Leap Frog Practice

- 1. A circle is inscribed in the isosceles triangle with respective side lengths 6, 6 and 4. Determine the area of the inscribed circle.
  - (a)  $\pi/2$
  - (b)  $3\pi/2$
  - (c)  $5\pi/2$
  - (d)  $7\pi/2$
  - (e) None of these
- 2. Quadrilateral ABCD in the Cartesian plane is pictured below. Determine the area enclosed by ABCD. (You may assume b > a and c > d as pictured.)



- 3. What is the volume of the cube that circumscribes the sphere that circumscribes the cube that circumscribes the sphere of radius 1 inch?
  - (a)  $9\sqrt{3}$  in<sup>3</sup>
  - (b)  $16\sqrt{2} \text{ in}^3$
  - (c)  $24\sqrt{3}$  in<sup>3</sup>
  - (d)  $54\sqrt{2}$  in<sup>3</sup>
  - (e) None of these
- 4. What is the value of a so that the vertical line x = a divides the triangle  $\triangle ABC$  pictured below into two regions of equal area?
  - (a)  $a = \sqrt{7}$ (b)  $a = \frac{7}{2}$ (c) a = 3(d)  $a = 10 - 2\sqrt{10}$ (e) None of these



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- 5. In the figure below, the rectangle is a square, whose side lengths are all equal to the value a, and the circle is inscribed as pictured. Determine the radius, r, of the inscribed circle.
  - (a)  $r = a(\frac{\sqrt{2}}{2})$ (b)  $r = a(1 - \frac{\sqrt{2}}{2})$ (c)  $r = a(\sqrt{2} - 1)$ (d)  $r = a(2 - \sqrt{2})$ (e) None of these



- 6. Two  $2' \times 2'$  squares share the same center and one square is rotated  $45^{\circ}$  with respect to the other square (see picture below). Determine the shaded area that is enclosed by both squares.
  - (a)  $4\sqrt{2} 4$  ft<sup>2</sup>
  - (b)  $4\sqrt{2} + 4$  ft<sup>2</sup>
  - (c)  $2\sqrt{2} + 2$  ft<sup>2</sup>
  - (d)  $8\sqrt{2} 8 \text{ ft}^2$
  - (e) None of these



- 7. A circle is inscribed in a square. A square is inscribed in that circle. A second circle is inscribed in that square. What is the ratio of the area of the smallest circle to the area of the largest square?
  - (a)  $\pi/2$
  - (b)  $\pi^2/4$
  - (c)  $\pi/8$
  - (d)  $\pi^2/16$
  - (e) None of these



- 8. A cylinder with radius r and height h has volume 1 and total surface area 12. Compute  $\frac{1}{r} + \frac{1}{h}$ .
  - (a)  $\frac{1}{12}$
  - (b)  $\frac{1}{6}$
  - (c) 6
  - (d) 12