# MATH 100 

## Final Exam

December 15, 2014

## Name:

- No books, notes, or calculators are allowed.
- Please show all your work.
- Always explain your solutions and calculations.
- In each one of problems $1,3,4,9: 2$ extra points will be given for a second solution.

1. (6 points) Write a story problem that can be solved using the following proportion. Explain clearly what quantities are related in the proportion. Solve your problem using this proportion.

$$
\frac{15}{x}=\frac{32}{5}
$$

2. (4 points) Explain why the units digit of a perfect square (i.e. the square of an integer) cannot be equal to 2 .
3. (4 points) Mike asked Santa to bring him a book with 1234 pictures of animals. On Christmas, he found a book under his tree that said there were $20143_{5}$ animal pictures in it. Does the book contain more or fewer pictures than Mike wanted?
4. (6 points) For this problem, clearly show all steps of problem solving.

A carpenter has three large boxes. Inside each large box are two medium-sized boxes. Inside each medium-sized box are five small boxes. How many boxes are there altogether?
5. (4 points) Put the following numbers in increasing order:

$$
\pi, \quad \sqrt{\pi}, \quad \sqrt{3}, \quad \sqrt{7}, \quad \frac{62}{20}
$$

6. (6 points) A rectangular prism with a square base has height 4 cm and volume $49 \mathrm{~cm}^{3}$. Find its surface area.
7. (6 points) For this problem, clearly show all steps of problem solving. I am thinking of a number. One third of my number minus a half of that same number is equal to 9 . What is my number?
8. (4 points) Find the greatest common factor of $2^{2014}$ and $2014^{2}$.
9. (6 points) Two right triangles are similar. One has hypotenuse 1 ft and area $0.2 \mathrm{ft}^{2}$. The second triangle has hypotenuse 25 ft . What is the area of the second triangle?
10. (4 points) Which of the following numbers are rational numbers but not integers?

$$
-\frac{4}{2}, \quad \sqrt{10}, \quad 3.14, \quad \frac{\sqrt{2} \sqrt{8}}{3}
$$

