## **MATH 110**

## Final Exam Study Guide

The final exam will be 2 hours long and will consist of 8-12 problems/questions (some with multiple parts).

The exam is cumulative, so review all the concepts, properties, and examples covered in this course. Use the following list as a guide. It is also a good idea to review all homework and exam problems.

- 1. Truthtellers and liars puzzle.
- 2. Statements, truth values of statements.
- 3. Open statements.
- 4. Logical connectives (operations).
- 5. Truth tables.
- 6. Compound statements, order of operations.
- 7. Logical equivalence.
- 8. Expressing operations in terms of others.
- 9. Fundamental logical equivalences.
- 10. Proving other logical equivalences from the fundamental ones.
- 11. Tautology, contradiction.
- 12. More puzzles (knigths, knaves, tourists, their language, guessing numbers, and various puzzles about true and false statements).
- 13. Set, subset.
- 14. Cardinality of a set.
- 15. Power set.
- 16. Set operations.
- 17. Venn diagram.
- 18. Indexed collection of sets, operations with it.
- 19. Fundamental identities in set theory.
- 20. Proving a set identity.
- 21. Similarities between logical and set operations and identities.
- 22. Interpretation of formulas in sets.
- 23. Formulas valid in sets.
- 24. Quantifiers.
- 25. Negations of quantified statements.

- 26. Nested quantifiers.
- 27. Properties of quantified statements.
- 28. Proving quantified statements.
- 29. Non-constructive proofs.
- 30. Paradoxes in logic and set theory.
- 31. Axioms, Modus Ponens.
- 32. Sound and complete axiom systems.
- 33. Deriving tautologies from axioms.
- 34. Modal operators box and diamond, their interpretations.
- 35. Axioms, Necessitation Rule.
- 36. Proving formulas from axioms.
- 37. Modal logics, sublogic relationships.