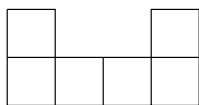
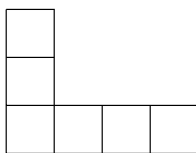


## Reveiw Problems

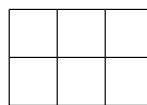
1. Find  $\frac{1}{2!} + \frac{2}{3!} + \frac{3}{4!} + \dots + \frac{n-1}{n!}$ .
2. Prove that if  $p > 3$  is prime, then  $p^2 \equiv 1 \pmod{24}$ .
3. There are 8 people in a room. Every person counted how many people he knows. (Assume that if  $A$  knows  $B$  then  $B$  knows  $A$ .)
  - (a) The numbers are 0, 1, 1, 2, 2, 3, 4, 4. Prove that somebody made a mistake.
  - (b) Can the numbers be 0, 1, 2, 3, 4, 5, 6, 7?
4. We strike the first digit of the number  $7^{2003}$ , and add it to the remaining number. This is repeated until a number with 10 digits remains. Prove that this number has 2 equal digit.
5. Show that it is not possible to cover any rectangle by one tile of type 1 shown below, one tile of type 2, and any number of tiles of type 3.



1



2



3

6. Let  $S$  be a set of 25 points such that, in any 3-subset of  $S$ , there are at least 2 points with distance less than 1. Prove that there exists a 13-subset of  $S$  which can be covered by a disk of radius 1.