## **MATH 145**

## Test 3

## 8 December 2003

Evaluate the integral (5 points):

• 
$$\int_{-4}^{2} |x+2| dx$$
 (use next page)

and do any 3 of the following problems (15 points each):

- 1. Two circles, S and T, and a point A are given. Find points B on S and C on T such that  $\triangle ABC$  is isosceles with AB = AC,  $\angle ABC = \angle ACB = 75^{\circ}$ , and  $\angle BAC = 30^{\circ}$ . Assume that a solution exists.
- 2. Find integer numbers a and b such that 6 = 67a + 25b.
- 3. Two players play the following game.
  - Turns alternate.
  - At each turn, a player removes either 1 or 2 counters from a pile that had initially 10 counters.
  - The game ends when all counters have been removed.
  - The player who takes the last counter loses.

Find a winning strategy for one of the players.

- 4. The parabola  $y = x^2 + 2$  has two tangent lines that pass through the origin. Find their equations.
- Extra credit (15 points): Two lines, p and q, and a point A are given. Find points B on p and C on q such that  $\triangle ABC$  is isosceles with AB = BC, and  $\angle ABC = 90^{\circ}$ . Assume that a solution exists.

• Evaluate the integral:  $\int_{-4}^{2} |x+2| dx =$ 

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**Extra credit:** Two lines, p and q, and a point A are given. Find points B on p and C on q such that  $\triangle ABC$  is isosceles with AB = BC, and  $\angle ABC = 90^{\circ}$ . Assume that a solution exists.