

# MATH 75B

## Test 1

February 21, 2018

Name: \_\_\_\_\_

- No books, notes, or calculators are allowed.
- Please show all your work for problems 7-10.
- Please simplify your answers whenever possible.

Multiple choice questions: circle the correct answer

1. Let  $f(x) = \arcsin(2x)$ . Find  $f'(x)$ .

A.  $\frac{1}{\sqrt{1-2x^2}}$

B.  $\frac{1}{\sqrt{1-4x^2}}$

C.  $\frac{2}{\sqrt{1-2x^2}}$

D.  $\frac{2}{\sqrt{1-4x^2}}$

E. none of the above

2. Let  $g(x) = x \ln x$ . Find  $g'(x)$ .

A.  $1 + \ln x$

B.  $\frac{1}{x}$

C.  $\ln x - 1$

D.  $\frac{e^x}{x}$

E. none of the above

3. The length of a rectangle is increasing at a rate of 8 cm/s and its width is decreasing at a rate of 3 cm/s. When the length is 20 cm and the width is 10 cm, how fast is the area of the rectangle increasing?

A.  $-24 \text{ cm}^2/\text{s}$

B.  $5 \text{ cm}^2/\text{s}$

C.  $20 \text{ cm}^2/\text{s}$

D.  $140 \text{ cm}^2/\text{s}$

E. none of the above

4. Find the critical number(s) of  $f(x) = x^2 - 6x$ .

A. 3

B. 6

C.  $\pm 6$

D. 0

E. none of the above

5. How many local maximum points does  $y = \sin x$  have?

A. 0

B. 1

C. 2

D. infinitely many

E. none of the above

6. How many inflection points does  $y = \ln x$  have?

A. 0

B. 1

C. 2

D. infinitely many

E. none of the above

**Regular problems: show all your work**

7. Consider the curve given by  $x^2 - 2xy + y^3 = 43$ .

(a) Use implicit differentiation to find  $y'(x)$ .

(b) Verify that the point  $(-2, 3)$  lies on the above curve.

(c) Find the slope of the tangent line to the above curve at the point  $(-2, 3)$ .

8. Car A is traveling north at 40 mi/h, and car B is traveling east at 50 mi/h. Both cars are approaching point P which is the intersection of the two roads. How fast is the distance between the two cars decreasing at the moment when car A is 30 mi and car B is 40 mi away from point P?

9. Find an equation of the tangent line to  $y = \tan^{-1} x$  at  $x = 1$ .

10. Let  $f(x) = \frac{x^2 + 4}{x}$ . Find the following.

(a) Domain of  $f(x)$

(b) Critical points of  $f(x)$ , if any

(c) Intervals of increase and decrease

(d) Local maximum and minimum points, if any

(e) Intervals of concavity

(f) Inflection points, if any