

Math 76**Practice problems for test 1**

1. For each function, find its inverse, and sketch the graphs of the original function and its inverse.

(a) $f(x) = e^x - 2$

(b) $f(x) = 2^{-x}$

(c) $f(x) = \ln(x + 3) + 2$

2. Find the exact value of

(a) $\log_5 \left(\frac{1}{125} \right)$

(b) $\log_6 2 + \log_6 3$

(c) $3 \log_8 4$

(d) $\arcsin(1)$

(e) $\arccos \left(\frac{1}{2} \right)$

(f) $\sin \left(\arctan \left(\frac{3}{4} \right) \right)$

3. Evaluate the limits.

(a) $\lim_{x \rightarrow 0} \frac{\sin 5x}{2 \sin 3x}$

(b) $\lim_{x \rightarrow 0} \frac{e^x (\cos x - 1)}{\tan(3x)}$

(c) $\lim_{x \rightarrow 0} \frac{e^x - 1 - x}{x^2}$

(d) $\lim_{x \rightarrow \infty} x^3 e^{-3x}$

(e) $\lim_{x \rightarrow \infty} \left(\frac{x}{x+1} \right)^{3x}$

4. Evaluate the following integrals.

(a) $\int x \sin(x^2) dx$

(b) $\int_{\pi/6}^{\pi/2} \cos^2 x dx$

(c) $\int \frac{4x+3}{x+1} dx$

(d) $\int_1^2 x e^x dx$

(e) $\int_0^{\pi} \sin^5 t dt$

(f) $\int_0^{\pi/4} \sec^2 x e^{\tan x} dx$

(g) $\int x^2 \sin(2x) dx$

(h) $\int \frac{1}{x^2 \sqrt{4-x^2}} dx$

(i) $\int \frac{7x+12}{x^3+4x^2} dx$

(j) $\int (\ln(5x))^3 dx$

(k) $\int \frac{4x+3}{x^2+1} dx$

(l) $\int (\cos x)^3 (\sin x)^2 dx$

(m) $\int \frac{1}{(2-3s)^5} ds$

(n) $\int \frac{1}{\sqrt{x^2+9}} dx$

(o) $\int \frac{e^x+5}{e^x+3} dx$

(p) $\int \frac{x^2}{x^2+5x+6} dx$

(q) $\int x \sqrt{4x^2-1} dx$